

19/42

Wed. Oct. 10

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• So far we have discovered that the discrete nature of solids leads to properties that would not arise in continuous media

e.g. • specific heat of solids @ low  $T$

• non-linearity & banding in the dispersion relations of phonons

• although we have talked some about banding in solids arising from electrostatics, we have not spent much time discussing ordering in solids

• often the lowest energy config. is a crystal with periodicity that is regular

• we saw the effect of periodicity for phonons which scatter strongly as  $\lambda \rightarrow a$ , where 'a' is the periodicity of the crystal

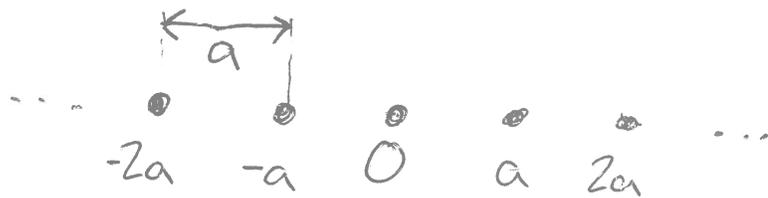
(2)

- Crystallography is an extensive topic & a critical aspect of the field is that it is independent of the properties of the atoms

### \* Crystal structure: Some definitions

- lattice: an infinite set of points defined by integer sums of a set of non-colinear lattice vectors

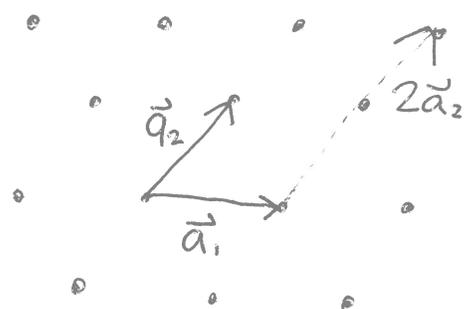
- We have seen a lattice before in the 1D solid where 'a' is the equilibrium spacing



- the points of the lattice are given by  $R = na$  (eq. positions)

- in 2D, for example
- points are at location

$$\vec{R}[n_1, n_2] = n_1 \vec{a}_1 + n_2 \vec{a}_2$$
$$n_1, n_2 \in \mathbb{Z}$$



- Without plotting points, we extrapolate to 3D

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$$\vec{R}[n_1, n_2, n_3] = n_1 \vec{a}_1 + n_2 \vec{a}_2 + n_3 \vec{a}_3$$

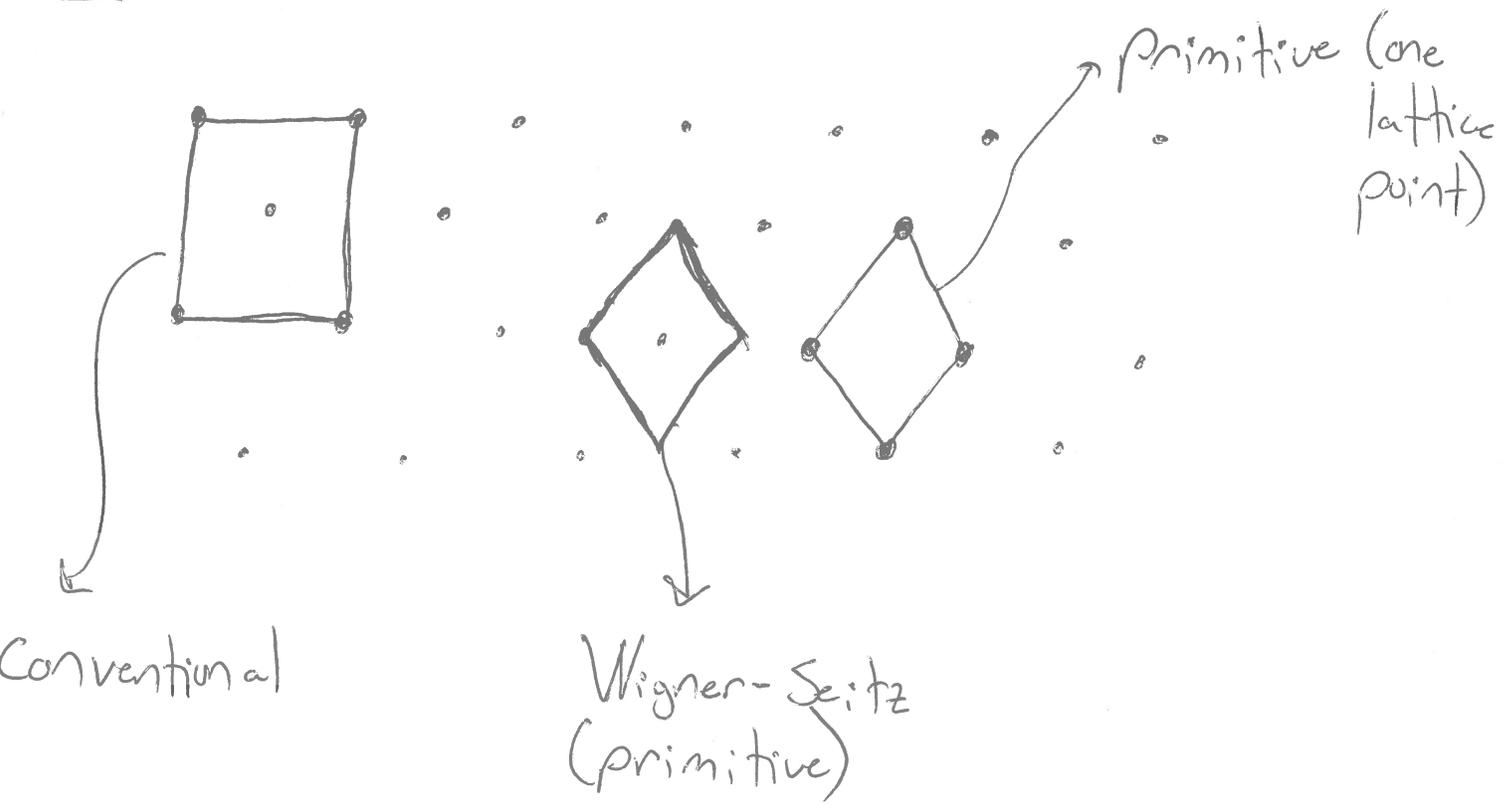
$$n_1, n_2, n_3 \in \mathbb{Z}$$

- Clearly, the addition of any two vectors in the set gives another vector in the set  
→ translational symmetry
- We have assumed a perfect periodic crystal, which do not exist in nature (even crystal face destroys periodicity)
- Thermal vibrations translate atoms away from lattice points (equilib. positions)
- Foreign atoms always present (best technologies  $\sim 10^{12}/\text{cm}^3$ )
- Foreign atoms have profound consequences for technologies

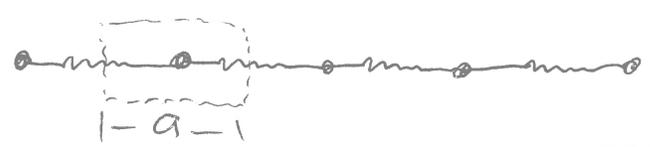
• The unit cell: a spatial region with the property that when identical units are "packed" together, it "tiles" and reconstructs the entire cell

• Primitive cell: only one lattice point in the cell (a unit cell)

• Unit cells are not unique

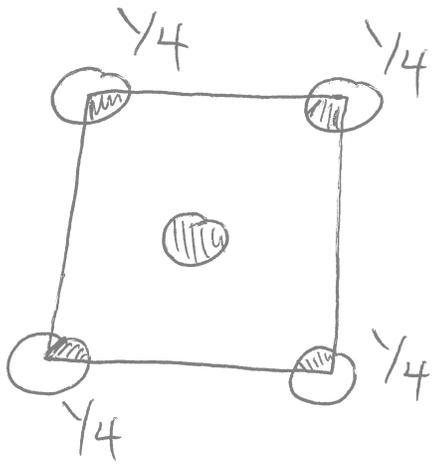


• Ex: for 1D case, primitive cell is not unique but must be of length 'a'



\* Notice something about the # of lattice points in a cell

Ex: conventional



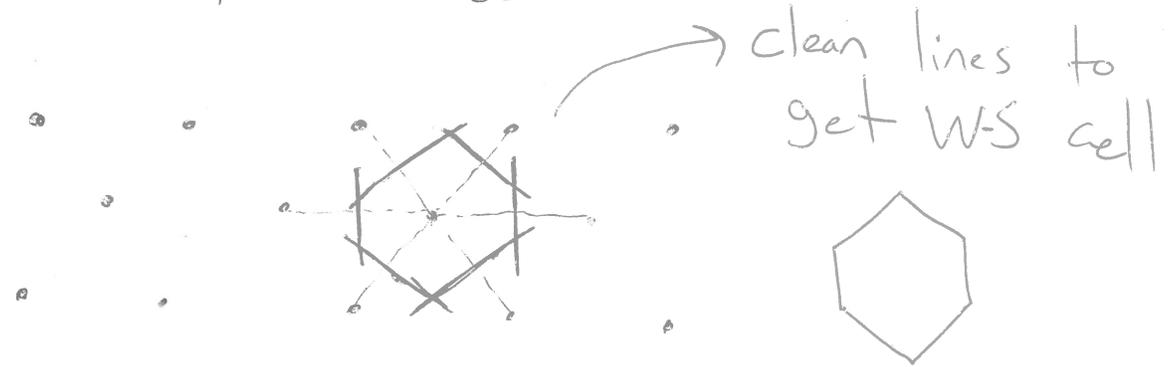
• # points in a cell =  $\frac{1}{4}(4) + 1 = 2$

$\uparrow$                      $\uparrow$   
 edges                center

- not a primitive cell (2-points)
- for Wigner-Seitz cell, all points in space of cell are closer to lattice point than other points (within lines)

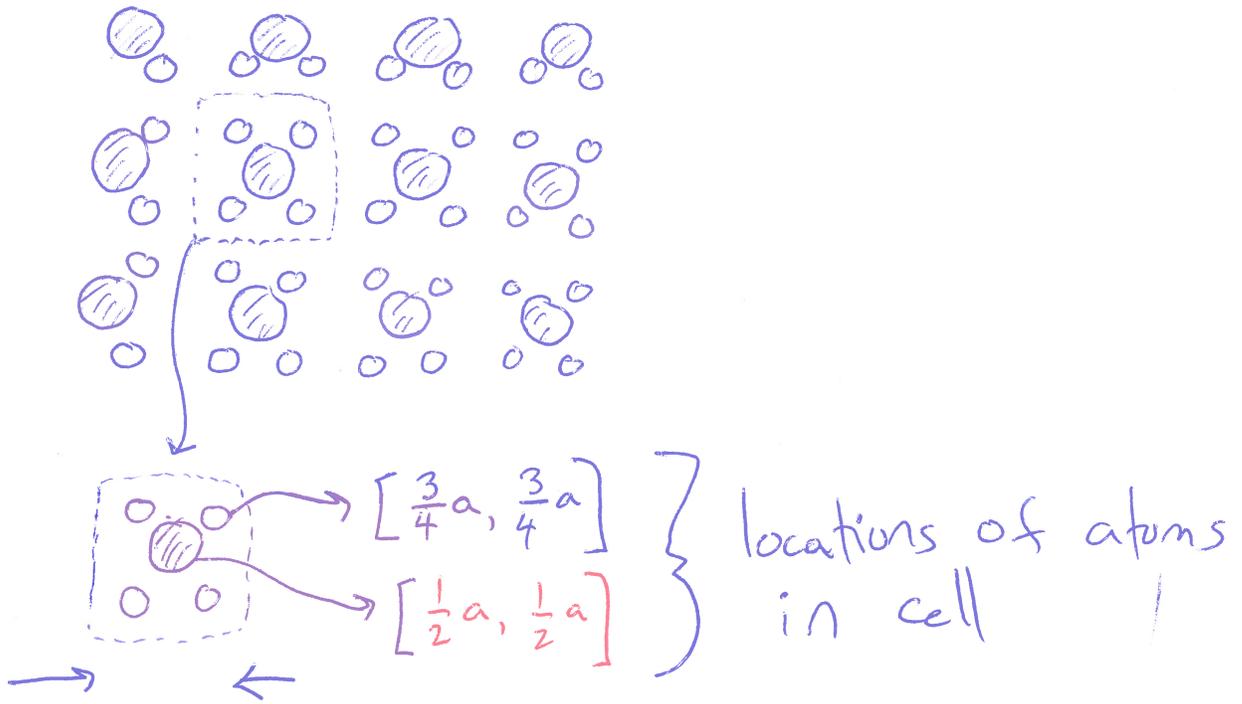
construction: draw lines to nearest neighbors, then bisect these lines at their midpoints w/  $\perp$  lines

Ex:



• Basis: description of objects within unit cell with respect to the lattice point within cell

Ex:



• Bravais lattice: all lattice points are equivalent

- for non-Bravais lattices, the points may be geometrically different or different atoms

