

12/42

Mon. Sept. 24

①

- Our free electron model worked well to approximate many physical phenomena involving conductors, but it has many limitations
- For example, how do we explain the behavior of insulators and semiconductors?
- to understand these effects, we need to know the details of the microscopic solid - i.e. what are the forces holding the solid together & how do they influence behavior?
- many solids consist of highly symmetric repeating units - these symmetries make modelling practical
- in other words, we are interested in crystals
- what binds a crystal?
- first, the crystal is typically the lowest energy state (at least locally)
- Ex: non-crystalline solids may be glasses

②

• let's just name the types of bonds:

- ionic
- covalent
- metallic
- molecular
- hydrogen

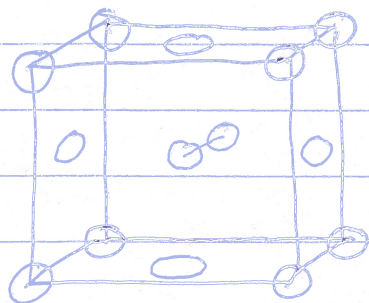
} all are electrostatic phenomena

• as a starting point, let's take an inert gas & cool it until it solidifies

• the inert gasses have very low melting points; atoms are weakly bound; transparent & electrically insulating; very high ionization energies

• let's use the example of argon (Ar)

• Ar atoms pack tightly in a solid in a "face-centered cubic" (fcc) crystal (melting temp. $\sim 80\text{K}$)



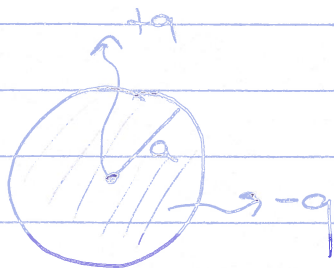
FCC

③

- What actually binds two atoms of Ar together?

- charge distribution of Ar is roughly symmetric (assume it is)

- $+q$ nucleus & $-q$ charge shell
(combined charge of electrons)



- from Gauss' law: $\oint \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0}$

- the field of nucleus holds electrons in orbit, but outside?

- $r > a$, we have $\oint \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0} = 0$

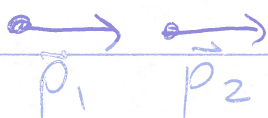
- and so $\vec{E} = 0$

- how does one atom affect another (via electrostatics) if $\vec{E} = 0$?

④

• the answer is that the charge density does not stay constant in time & so the atom becomes a fluctuating dipole, $E \neq 0$

• a non-zero field induces a dipole in a nearby atom & the two attract

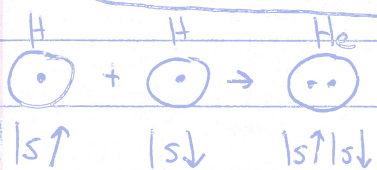


• this attractive force goes like $1/r^6$, where r is the distance between atoms

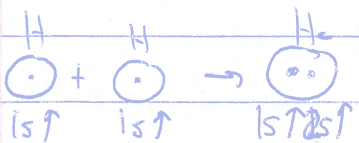
• by Pauli exclusion principle, there is a repulsive term also $1/r^{12}$

$$U(r) = 4E \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]$$

repulsion:



e^- energy = -78.98 eV



e^- energy = -59.38 eV

• repulsion ~ 20 eV from exc. princ.

→ repulsive

• Lennard-Jones

potential

$r = r_0$

→ attractive

⑤

• What is significant about r_0 ?

• When summing over all interacting atoms in crystal, we can determine the lattice constant by setting

$$\frac{dU_{\text{tot}}}{dr} = 0$$

• which gives $\frac{r_0}{a} \approx 1.09$

• measured values:

Ne	Ar	Kr	r_0/a
1.14	1.11	1.10	

• Ionic crystals: e.g. NaCl

• energy is needed to ionize a Na atom

Energy in: $\text{Na} + \sim 5.1 \text{ eV} \rightarrow \text{Na}^+ + e^-$

out: $e^- + \text{Cl} \rightarrow \text{Cl}^- + \sim 3.6 \text{ eV}$

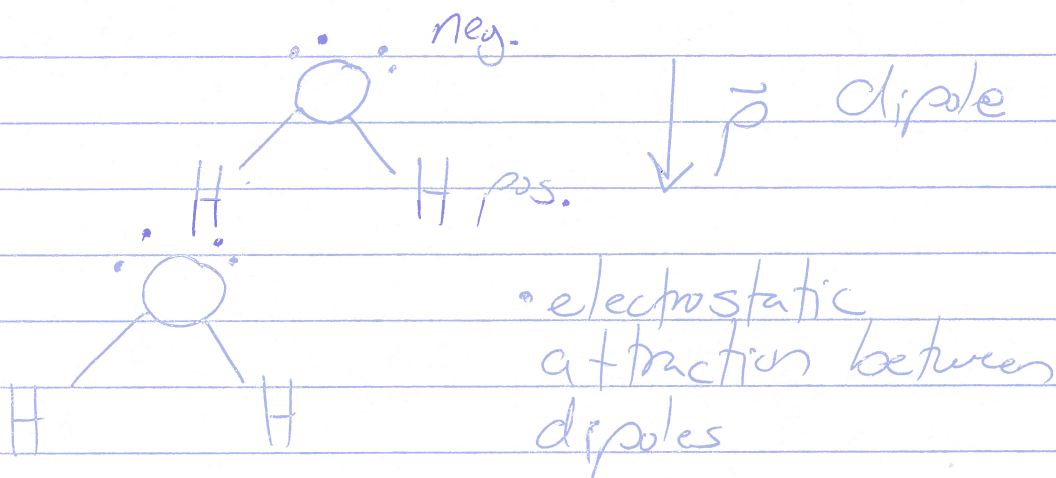
out: $\text{Na}^+ + \text{Cl}^- \rightarrow \text{NaCl} + \sim 7.9 \text{ eV}$

"cohesive energy" $\sim 7.9 \text{ eV}$ (needed to separate ions)

total: $(7.9 + 3.6 - 5.1) \text{ eV} = 6.4 \text{ eV}$

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Hydrogen bonding: arising from permanent dipoles in molecules



- eg. ice from water is due to H-bonding
- Metallic bonding: why are the valence electrons "loosely" bound in a metal?
The ionic (+) charge is screened by other electrons (core electrons)
- Na atoms have a single valence electron - how does the valence electron contribute to bonding?
- Again, the total energy is reduced when the electrons have a larger volume to move - more atoms, lower energy

